To find the focal length of a concave lens using a convex lens.
APPARATUS AND MATERIAL REQUIRED
Convex lens ( $\sim 15 \mathrm{~cm}$ )

* Focal length of convex lens should be smaller than the focal length of concave lens

PRINCIPLE
As the image formed by a concave lens is always virtual and erect, so, its focal length cannot be determined directly. However, it can be determined by introducing a convex lens in between the object and the concave lens.


- A convex lens $L_{1}$ converges the light rays starting from the object $A B$ to form a real and inverted image $A^{\prime} B^{\prime}$ at position $\mathrm{I}_{1}$ [Fig. (a)].
- If a concave diverging lens $L_{2}$ is inserted between the lens $L_{1}$ and point $I_{1}$ as shown in Fig. (b), for concave lens $L_{2}$ image $A^{\prime} B^{\prime}$ behaves as virtual object.
- A real and inverted image $A^{\prime \prime} B^{\prime \prime}$ is formed at point $I_{2}$ by the diverging lens $L_{2}$. Thus, for the concave lens $L_{2}$ the distances $O^{\prime} l_{1}$ and $O^{\prime} l_{2}$ would be the distances $u$ and $v$, respectively.
- It is important to note that the focal length of convex lens $L_{1}$ must be smaller than the focal length of the concave lens $\mathrm{L}_{2}$.
- The second image $A^{\prime \prime} B^{\prime \prime}$ is formed only when the distance between lens $L_{2}$ and first image $A^{\prime} B^{\prime}$ is less than the focal length of $L_{2}$.
- The focal length of the concave lens $L_{2}$ can be calculated from the relation $\frac{1}{v}-\frac{1}{u}=\frac{1}{f}$ or $f=\frac{u v}{u-v}$ For concave lens both ' $u$ ' and ' $v$ ' are positive and since $u<v$, $f$ will always be negative.

PROCEDURE

1. In case, if the focal length of the given thin convex lens is not known then rough value of its focal length $\left(f_{\mathrm{L}}\right)$ should be estimated first to ensure that its focal length is less than that of the concave lens.
2. Place the optical bench on a rigid platform and make it horizontal with the help of levelling screws provided at the base of the bench.
3. Place the uprights mounted with pin $P_{1}$ (object pin), convex lens $L_{1}$, and another pin $P_{2}$ (image pin) on the optical bench. You may put a small piece of paper on image pin $P_{2}$ to differentiate it from the image of object pin $\mathrm{P}_{1}$ [Fig. (a)]
4. Check the collinearity of the tip of pin $P_{1}$, optical centre $O$ of convex lens $L_{1}$, and the tip of image pin $P_{2}$ along a horizontal straight line, which is parallel to the length of the optical bench.
5. Separate object pin $\mathrm{P}_{1}$ from the convex lens by a distance slightly greater than the focal length $f_{\llcorner }$of the lens.
6. Locate its real and inverted image at point $\mathrm{I}_{1}$ on the other side of the lens by removing the parallax between the image pin $\mathrm{P}_{2}$ and image of the object pin $\mathrm{P}_{1}$ [Fig. (a)].

(a)

(b)
7. Read the positions of the uprights holding the object pin $P_{1}$, convex lens $L_{1}$, and image pin $P_{2}$ (i.e. point $I_{1}$ ). Record these observations in observation table.
8. From now on, do not change the position of the convex lens $L_{1}$ and the position of the object pin $P_{1}$. Insert the concave lens $L_{2}$ in between the convex lens $L_{1}$ and image pin $P_{2}$. Now the image of object pin will shift further from the convex lens $L_{1}$ to a point $I_{2}$ (say). Adjust the position of the concave lens so that the point $I_{2}$ is sufficiently away from the point $\mathrm{I}_{1}$.
9. In case the image formed by the combination of convex and concave lenses is not distinctly visible, try to see it on moving the concave lens nearer to the point $I_{1}$ and to locate the image by using a pencil held in hand, and keeping the image pin $P_{2}$ at point $I_{1}$ as a guide to decide which way to shift the concave lens $L_{2}$. After having seen the clear image at point $I_{2}$ and ensured that it lies within the range of the optical bench, move image pin $\mathrm{P}_{2}$ to locate the image (or point $\mathrm{I}_{2}$ ) more accurately using the method of parallax [Fig. (b)]. Since the image forming at $I_{2}$ is quite enlarged, it can be blurred.
10. Note the position of uprights holding the concave lens and image pin $P_{2}$, i.e., point $\mathrm{I}_{2}$. Note the readings in the Observation Table.
11. Change the position of upright holding the object pin $P_{1}$ and repeat the steps 6 to 11 . Take five sets of observations.

Link: https://youtu.be/Ye4K FpQ5rM (best) / https://youtu.be/mnMuCkFiMkg / https://youtu.be/V8nS4IzZkU8

## OBSERVATIONS

1. Focal length of the convex lens, $f_{L}$ (estimated/ given) $=\ldots \mathrm{cm}$
2. Length of the index needle, $\mathrm{s}=\ldots \mathrm{cm}$

## Determination of $\mathbf{u}, \mathbf{v}$ and f of concave lens

| S.No. | Upright position of |  |  |  |  | Observed$\begin{gathered} u=c-d \\ (\mathrm{~cm}) \end{gathered}$ | Observed$\begin{gathered} v=g-d \\ (\mathrm{~cm}) \end{gathered}$ | Focal <br> length $f(\mathrm{~cm})$ | $\Delta f$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { Object } \\ \text { pin } \\ \text { a(cm) } \end{gathered}$ | Convex <br> lens $\mathrm{L}_{1}$ <br> b(cm) | Image formed by $\mathrm{L}_{1}$ c(cm) | Concave <br> lens $\mathrm{L}_{2}$ <br> $\mathrm{d}(\mathrm{cm})$ | Image formed by combination $\mathrm{g}(\mathrm{cm})$ |  |  |  |  |
| 1 |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Mean |  |  |

## CALCULATIONS

- Calculate the focal length of the concave lens using the following relation, $f=\frac{u v}{u-v}$
- Error: $\Delta f=f^{2}\left[\frac{\Delta v}{v^{2}}+\frac{\Delta u}{u^{2}}\right]$ where $\Delta u$ and $\Delta v$ are the least counts of the measuring scale.


## RESULT

The focal length of the given concave mirror is $f \pm \Delta f=\ldots \mathrm{cm}$ (here $f$ is mean value of the focal length)

## PRECAUTIONS (ANY TWO)

1. The concave lens must be placed near the convex lens (In fact, the second image $\mathrm{I}_{2}$ is formed only when the distance between concave lens $L_{2}$ and first image $I_{1}$ is less than the focal length of the concave lens).
2. Since the image formed at $I_{2}$ is quite enlarged, it can be blurred. Therefore, it would be preferable to use a thin and sharp object pin and shine it with light using a lighted electric bulb.
3. The convex lens and the pin $\mathrm{P}_{1}$ must not be disturbed during the second part of the experiment.
4. A diminished, real and inverted image of the image pin $P_{2}$ might also be formed by the light rays reflecting from the concave surface of the lens $L_{2}$. It should not be confused with the bold and bright image formed by the combination of convex and concave lenses.

## SOURCES OF ERROR

1. If tip of object pin and optical centre of the lens are not aligned properly (if not brought at the same horizontal level), image tip and image of object pin tip will not touch each other.
2. For greater accuracy, we should use sharply pointed object pin.
